Hierarchical Reinforcement Learning under Mixed Observability

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Abstract. The framework of mixed observable Markov decision processes (MOMDP) models many robotic domains in which some state variables are fully observable while others are not. In this work, we identify a significant subclass of MOMDPs defined by how actions influence the fully observable components of the state and how those, in turn, influence the partially observable components and the rewards. This unique property allows for a two-level hierarchical approach we call HIerarchical Reinforcement Learning under Mixed Observability (HILMO), which restricts partial observability to the top level while the bottom level remains fully observable, enabling higher learning efficiency. The top level produces desired goals to be reached by the bottom level until the task is solved. We further develop theoretical guarantees to show that our approach can achieve optimal and quasi-optimal behavior under mild assumptions. Empirical results on long-horizon continuous control tasks demonstrate the efficacy and efficiency of our approach in terms of improved success rate, sample efficiency, and wall-clock training time. We also deploy policies learned in simulation on a real robot.

Keywords: Robot Learning, Hierarchical, Mixed Observability

1 Introduction

Many robotic domains feature a state space that factorizes into high and low observability subspaces, in which actions primarily influence the high observability components of the state. For example, robot navigation with unknown dynamics and noisy sensors to an unknown dynamic target [5] (Fig. 1a), or robot manipulation to reach an unknown target pose, *e.g.*, find an object in cluttered and occluded environments [29] (Fig. 1b), grasp under uncertainty [13], or collaborate with humans with partially observed human factors (*e.g.*, trust [3], preferences [27], or goals [21]). In these examples, state variables such as a robot's position or an arm's pose can be measured with high accuracy (*e.g.*, using GPS signals and sensors) than partially observable variables relative to the task and

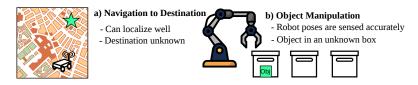


Fig. 1: Examples of partially observable domains of our interests.

are often assumed fully observable. Moreover, actions directly influence the fully observable state components and indirectly affect partially observable ones. For example, in Fig. 1, navigation actions can lead the mobile robot to different locations that contain useful information to reach the destination; sequences of poses help the robot arm open boxes to examine which contains the object.

Our contributions are as follows. First, we formulate such tasks using the framework of mixed observability Markov decision process (MOMDP) [22] and define motion-based MOMDPs (MOB-MOMDPs), a subclass of MOMDPs which makes mild assumptions concerning dynamics and tasks. Second, we introduce a hierarchical solution to solve MOB-MOMDPs, consisting of a high-level policy with partial observability and a low-level policy with full observability. In our agent, the top policy uses high-level observations to compute the bottom policy's goals, which are desired points in the fully observable space. When the bottom policy achieves a given goal or times out, emitted observations are used to produce the next high-level observation for selecting the next goal, and so on. Our approach can potentially offer efficient learning by breaking a long-horizon task into easier-to-learn subtasks, which enjoy full observability. Moreover, a hierarchical approach would explore more efficiently when rewards are sparse, thanks to high-level actions. In both theory and empirical experimentation, we show that our proposed hierarchical approach can achieve optimal or quasi-optimal behavior in MOB-MOMDPs with sufficiently low stochasticity constraints.

We demonstrate the benefits of our approach on long-horizon simulated continuous control domains with sparse rewards. Such domains are challenging for many non-hierarchical POMDP methods [9, 19]. In contrast, our hierarchical agent achieves higher success rates with excellent efficiency in training samples and wall-clock training time. Further, our robot experiments show that a learned policy could be effectively deployed in the real world.

2 Background

In this section, we will first go through the background of a goal-conditioned MDP (which will be solved by the bottom level), then the frameworks of partially observable Markov decision processes (POMDP) and MOMDP. We conclude by the hierarchical reinforcement learning algorithm that our approach builds upon.

A goal-conditioned MDP is defined by a tuple (S, A, G, T, R, γ) , where S is the state space, A is the action space, G is the goal space, $T : S \times A \to S$ is the

transition function, $R: S \times A \times G \to \mathbb{R}$ is the reward function, and $\gamma \in [0, 1)$ is the discount factor. The objective is to find a goal-conditioned policy $\pi: S \times G \to \Delta A$ which maximizes the return $\mathbb{E}_{\pi}[\sum_{t=0}^{\infty} \gamma^t r_t]$, where r_t is the reward at timestep t.

A **POMDP** [2] is specified by a tuple $(S, A, T, R, \Omega, O, \gamma)$, where (S, A, T, R, γ) are the same as in a goal-conditioned MDP. Instead of directly observing the state s, the agent only observes $o \in \Omega$ after taking an action a and reaching state s' governed by the observation function $O(s', a, o) = p(o \mid s', a)$. The goal is to find a policy π that maximizes the expected discounted return defined as $\mathbb{E}_{\pi}[\sum_{t=0}^{\infty} \gamma^{t}r_{t}]$. To take an optimal action at timestep t, an agent often must condition its policy on the entire action-observation history $h_{t} = (o_{\leq t}, a_{< t}) \in \mathcal{H}_{t}$ that it has seen so far. However, the size of the history \mathcal{H}_{t} grows exponentially with t. Therefore, a recurrent neural network (RNN) is often used to summarize h_{t} with its fixed-sized hidden state.

A **MOMDP** [22] is a POMDP in which a state can be decomposed as s = (x, y), where $x \in \mathcal{X}$ is fully observable and $y \in \mathcal{Y}$ is partially observable. Since x is fully observable, an observation o can be decomposed as $o = (x, z) \in \Omega$ where z is the remaining component of o. The observation function

$$O(s', a, o) = p(o \mid s', a) = p(x, z \mid x', y', a) = \mathbb{1}[x = x']p(z \mid x', y', a)$$
(1)

specifies which observation the agent gets after it took action a and reached state s' = (x', y') with 1 denoting the indicator function. The transition function T(s, a, s') = p(s' | s, a) = p(x', y' | x, y, a) for $x, x' \in \mathcal{X}$ and $y, y' \in \mathcal{Y}$ specifies the probabilities of reaching a state (x', y') after taking an action a in state (x, y). T(s, a, s') can be decomposed as

$$T(s, a, s') = p(s' \mid s, a) = p(x', y' \mid x, y, a) = p(x' \mid x, y, a)p(y' \mid x, y, a, x').$$
(2)

Let $T^{\mathcal{X}}(x, y, a, x') = p(x' \mid x, y, a)$ and $T^{\mathcal{Y}}(x, y, a, x', y') = p(y' \mid x, y, a, x')$, the tuple $(\mathcal{X}, \mathcal{Y}, \mathcal{A}, T^{\mathcal{X}}, T^{\mathcal{Y}}, R, \Omega, O, \gamma)$ formally defines a MOMDP.

Hierarchical Actor-Critic (HAC) [16] is an MDP hierarchical agent, in which an action from a non-base level is a goal for the policy at the level right below it, and the base policy will directly interact with the environment. The policies in each level are trained in an off-policy manner using replay buffers, one for each level. We build our agent upon a two-level HAC agent and utilize different techniques in HAC to stabilize the training at the top level and learn effectively under sparse rewards at the bottom. More details are in Section 4.

3 Motion-Based MOMDPs

We define motion-based MOMDPs (MOB-MOMDPs) as MOMDPs which satisfy the following additional factorization and independence assumptions,

$$p(s' \mid s, a) = p(x' \mid x, a)p(y' \mid x, y, x'),$$
(3)

$$p(o \mid s', a) = p(o \mid s'),$$

$$(4)$$

$$P(o \mid s', a) = P(o \mid s'),$$

$$(5)$$

$$R(s,a) = R(s).$$
⁽⁵⁾

In other words, a) the fully observable component x of the state satisfies the Markov property without depending on the partially observable component y of the state, b) both the partially observable component y of the state and the observed component z are conditionally independent on the action a (when conditioned on the fully observable component x of the state), and c) the task is encoded by a reward function which exclusively depends on the reached states, and not the actions taken. We refer to MOB-MOMDPs, which have deterministic (stochastic) $T^{\mathcal{X}}$ as deterministic (stochastic) MOB-MOMDPs; note that this does not refer to the stochasticity of $T^{\mathcal{Y}}$, which remains unconstrained.

In MOB-MOMDPs, actions only have a direct influence on the resulting x trajectories, while their influence on the y, z, and reward trajectories is indirect through x. MOB-MOMDPs include (but are not limited to) navigation tasks where x represents the fully observable pose of the agent in the environment, while y represents other partially observable information about the environment and task. In such navigation MOB-MOMDPs, actions relate to the *motion* of the agent, and it is exclusively through such motion that the agent is able to interact with the environment, gather information, and complete the task. Although not all MOB-MOMDPs intrinsically represent navigation tasks, we will use the imagery of navigation tasks as a useful analogy to simplify the way we discuss and analyze MOB-MOMDPs and the respective learning algorithms. Therefore, we reinterpret general MOB-MOMDPs as navigation tasks where x figuratively represents the agent's pose, a the movements that allow the agent to change its pose, and y as any other partially observable aspect concerning the task.

Using such analogy, and because actions exclusively influence the environment through the resulting agent pose, it is possible to abstract "motion"-based control (*i.e.*, based on the actions which move the agent) as "pose"-based control (*i.e.*, based on the poses which the agent should reach in order to gain information or complete the task). "Pose"-based control is executed not by choosing how the agent should move (action a), but rather where it should move to (pose x'). Such abstraction is the inspiration for a flavor of hierarchical reinforcement learning specifically suited to solve MOB-MOMDPs.

4 Hierarchical Reinforcement Learning under Mixed Observability

We first give an overview of our hierarchical method, and how each hierarchy layer is trained. Then we provide an optimality analysis of the approach.

4.1 Approach

Overview. As shown in Fig. 2, HIerarchical reinforcement Learning under Mixed Observability (HILMO) makes decisions through a two-level hierarchy. The top-level policy is a recurrent module (symbolized by an arrow pointing to itself) which takes in a top-level observation o_t^T (a summary of several past primitive observations $o \in \Omega$) to produce a goal $x_t^T \in \mathcal{X}$ being the desired value

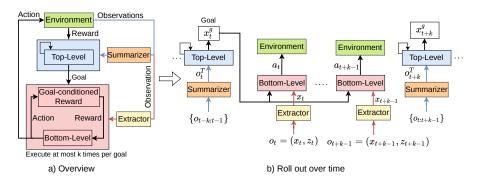


Fig. 2: Our two-level hierarchical agent. A memory-based top-level policy looks at a summary of several past observations to select a desired state (goal) x_t^g for the bottom-level policy. A memoryless bottom policy then looks at x_t (a component of observation $o_t = (x_t, z_t)$) and the goal state x_t^g to produce at most k primitive actions to achieve x_t^g , emitting a new sequence of observations. Next, these observations will be fed to a summarizer to create a new high-level observation for the top policy to select a new goal.

for x_t . Then the memoryless bottom-level policy selects an action a_t using x_t (extracted from $o_t = (x_t, z_t)$) and x_t^g . Notice this also covers the case when we want to set the goal only for a subspace of \mathcal{X} . For instance, although x of the mobile robot in Fig. 1 might include both positions and velocities, we might just want it to successfully reach a certain position regardless of its velocity.

The goal x_t^g remains unchanged until x_t^g is achieved or k bottom-level actions have been performed (for clean notations, from now, we assume that the bottom episode will always last k timesteps). When the bottom level finishes acting, kobservations $o_{t:t+k-1}$ (*i.e.*, o_t, \ldots, o_{t+k-1}) are emitted. These observations will be fed to a summarizer to create the next top-level observation o_{t+k}^T for the top policy to choose the next goal. In this hierarchy, the top level acts at a higher temporal resolution than the bottom level. For a complete algorithm of HILMO, please refer to Appendix A.

Bottom-Level. A bottom-level goal-conditioned MDP $\mathcal{M}^{\mathcal{X}}$ is specified by $(\mathcal{X}, \mathcal{A}, \mathcal{G} = \mathcal{X}, T^{\mathcal{X}}, R^{\mathcal{X}}, \gamma)$. The reward function $R^{\mathcal{X}}$ is defined for each goal $x^g \in \mathcal{X}$ as $R^{\mathcal{X}}(x', x^g) = -\mathbb{1}[d(x', x^g) \ge \epsilon]$, where d is some given distance metric in \mathcal{X} and ϵ is a small reaching threshold. The transition function $T^{\mathcal{X}}(x, a, x') =$ $p(x' \mid x, a)$ specifies the probabilities of reaching x' after taking action a in x. A goal-conditioned policy $\pi^{\mathcal{X}}(a \mid x, x^g)$ that solves $\mathcal{M}^{\mathcal{X}}$ will maximize the discounted cumulative reward $\sum_{t'=t}^{t+k-1} \gamma^{t'-t} R^{\mathcal{X}}(x_{t'}, x^g)$, where x_t is the starting state. The input x of $\pi^{\mathcal{X}}$ is from an extractor that extracts x from o = (x, z).

Top-Level. A top-level POMDP \mathcal{P}^T is specified by $(\mathcal{S}, \mathcal{A}^T = \mathcal{X}, T^T, R^T, \Omega^T, O^T, \gamma)$. In particular, its action space \mathcal{X} is the goal space in $\mathcal{M}^{\mathcal{X}}$, therefore a *top-level* policy $\pi^T(\cdot \mid o^T)$ that solves \mathcal{P}^T will output a desired state x^g to be reached by $\pi^{\mathcal{X}}$. The top-level transition function can be specified as a *multi-time*

6

model [23] that describes a multi-step policy taking in the goal a^T from state s

$$T^{T}(s, a^{T}, s') = \sum_{m=1}^{k} p(s', m \mid s, a^{T}), \qquad (6)$$

where $p(s', m \mid s, a^T)$ is the probability that the bottom policy $\pi^{\mathcal{X}}$ terminates at state s' after exactly m primitive actions when it acts to achieve the goal a^T starting from state s. Unlike $\pi^{\mathcal{X}}$, the objective of π^T is to optimize the discounted cumulative reward $\sum_{t=0;t+=k}^{\infty} \gamma^{t/k} R^T(s_t, a_t^T)$ where each $R^T(s_t, a_t^T)$ is the expected accumulated environment rewards when π^X acts for k timesteps to achieve the goal a_t^T starting at state s_t . Top-level observations are defined as the sequence of actions and observations obtained by the low-level policy until control is given back to the high-level policy, e.g., assuming that at time-step tthe high-level policy chooses goal $x^g = a^T$, and that the low-level policy interacts with the environment for k timesteps by choosing actions (a_t, \ldots, a_{t+k-1}) and receiving observations (o_t, \ldots, o_{t+k-1}) , then $o^T = (a_t, o_t, \ldots, a_{t+k-1}, o_{t+k-1})$.

4.2 Bottom-level Policy Learning

Because the bottom policy acts in a fully observable system with sparse rewards, we learn it using transitions sampled from a replay buffer using goal relabeling [1].

Goal Relabeling is a commonly used and powerful technique for learning under sparse rewards. We utilize the technique to replace unmet goals in past transitions with ones met in hindsight, creating positive learning signals as goals are met. Similarly, HAC uses goal relabeling to create hindsight goal transitions (HGT). Specifically, given a bottom-level transition (x, a, x', r, x^g) that did not reach x^g but reached x'^g instead, a modified transition (x, a, x', r', x'^g) where r' is the new reward associated with x'^g will be used for training. In contrast, if x^g is reached when the transition ends, the original transition will be used.

Learning Algorithm. Adopting HAC's choice, we use a version of DDPG [18] without target networks. We also experimented with other learning algorithms such as TD3 [7] and SAC [8], but none outperformed DDPG. Please see Appendix B for more details about our implementation of DDPG.

4.3 Top-Level Policy Learning

The top policy is trained off-policy using samples from a replay buffer of top-level episodes. This differs from HAC's memoryless top level, which can be trained using transitions. Here we introduce methods to create top-level observations and forming training episodes before describing the learning algorithm.

Creating Top-Level Observations. In practice, the summarizer applies an operator \mathcal{F} to k low-level observations to create a high-level observation. In this perspective, a high-level observation can be considered as an implication of temporally extended perception. Here, we consider three options for \mathcal{F} .

<u>Full.</u> Concatenating all k previous observations to create a top-level observation. If the bottom policy finishes before k timesteps, we simply pad zeros to have k observations.

<u>Final.</u> Using the final (k-th) observation as a top-level observation. This approach is commonly used in MDP hierarchical agents such as HAC and HIRO [20].

<u>Recurrent.</u> Using a separate and learnable recurrent layer to summarize all k previous observations with the final hidden state being a top-level observation.

Creating Stationary Training Episodes. Given a top-level episode in with any goal unachieved, using it directly to learn the top policy will cause non-stationarity. For instance, given the same (o^T, a^T) , the bottom policy can achieve other undesired goals, leading to multiple possibilities of (o'^T, r^T) . This makes learning $Q(o^T, a^T)$ at the top level non-stationary.

Creating Stationary Transitions: Stationary transitions are created using hindsight action transitions (HAT) [16], which are modified transitions as if the bottom policy already converges and always achieves its goals. Specifically, given a transition $(o^T, a_{\text{unmet}}^T, o'^T, r^T)$ with an unmet action (goal) a_{unmet}^T , the transition $(o^T, a_{\text{met-by-bottom}}^T, r^T)$ will instead be used, where $a_{\text{met-by-bottom}}^T$ is the goal reached by the bottom policy.

Penalizing Unachieved Goals: Producing unrealistic goals that are unreachable by the current bottom policy should be discouraged. Therefore, whenever the top policy produces an unachieved goal for the bottom policy, it will be penalized by a negative reward with some probability. Specifically, given a transition $(o^T, a^T_{\text{unmet}}, o'^T, r^T)$, the transition $(o^T, a^T_{\text{unmet}}, o'^T, -H^T)$ will be used, where H^T is the time horizon of the top policy. These transitions are known as subgoal testing transitions (STT) [16].

Forming Stationary Episodes: While HATs or STTs alone are sufficient to train a memoryless HAC agent, we must combine those transitions to form episodes for training our recurrent top policy. Fig. 3 illustrates a method transforming a nonstationary episode into its stationary versions. Here a top-level non-

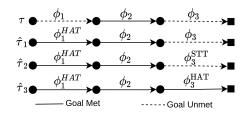


Fig. 3: Creating training episodes for π^T .

stationary episode τ comprises three transitions ϕ_1, ϕ_2 , and ϕ_3 in which a goal is only achieved (by the bottom policy) in transition ϕ_2 . We a) replace ϕ_1 with ϕ_1^{HAT} to create a stationary episode $\hat{\tau}_1$, b) use HAT for ϕ_1 and STT for ϕ_3 to create episode $\hat{\tau}_2$, or c) use HAT for ϕ_1 and ϕ_3 to create episode $\hat{\tau}_3$. Finally, three stationary episodes $\hat{\tau}_1, \hat{\tau}_2$, and $\hat{\tau}_3$ are used to train π^T .

Learning Algorithm. We use Recurrent Deterministic Policy Gradient (RDPG) [10] to learn the top-level policy with an LSTM [12] recurrent component. For the algorithm and the implementation details, see Appendix C. We also experiment with Gated Recurrent Unit (GRU) [4] and a recurrent version of TD3 [7] instead of RDPG (see Appendix D for a performance comparison).

4.4 Optimality Analysis

In this section, we analyze the optimality of the HILMO approach in MOB-MOMDPs, *i.e.*, whether the best HILMO policies are also guaranteed to achieve optimal MOB-MOMDP behavior. As it turns out, the amount of stochasticity of the MOB-MOMDP (as defined in Section 3, *i.e.*, only concerning $T^{\mathcal{X}}$) becomes a determining factor on the optimality of the HILMO approach. Initially, we will assume *deterministic* MOB-MOMDPs, and show that optimality is guaranteed.

Theorem 1. For deterministic MOB-MOMDPs and sufficiently large γ , the optimal HILMO policies are optimal or quasi-optimal for the MOB-MOMDP.

Proof. We first assume $\gamma = 1$, and show by construction that optimal MOB-MOMDP policies can be represented as HILMO policies, and then show that no other HILMO policies are preferable according to the HILMO criteria.

Consider, without loss of generality, a deterministic optimal policy π^* for the deterministic MOB-MOMDP. Next, we show that we can construct a HILMO policy which exhibits the same optimal behavior. Given any history h and its associated fully observable pose x, the optimal policy selects action $a = \pi^*(h)$ which causes a transition into pose x'. Due to the deterministic assumptions on $T^{\mathcal{X}}$ and π^* , each h is associated with a unique resulting transition (h, x, a, x'). Consider the HILMO policy (π^T, π^X) constructed such that for each such tuple $(h, x, a, x'), \pi^T(h) = x'$ and $\pi^{\mathcal{X}}(x, x') = a$, while all other actions $\pi^{\mathcal{X}}(x, g)$ can be chosen to achieve the shortest path between x and g to satisfy the low-level MDP optimality criterion. Such HILMO policy exhibits the exact same behavior as the optimal policy π^* , *i.e.*, for all histories h the equality $\pi^{\mathcal{X}}(x, \pi^T(h)) = \pi^*(h)$ holds. This shows that any behavior which is optimal for the control problem can be represented as a HILMO policy. To conclude, we need to show that there is no other HILMO policy that would be preferable to the one constructed according to the HILMO criteria of optimality for the low-level and high-level policies respectively. This is trivial for the constructed low-level policy, which effectively already finds the shortest (i.e., one-step) path between two poses x and x', and for the constructed high-level policy, which shares the same optimality criterion as the original MOB-MOMDP.

When $\gamma < 1$, the HILMO top-level criterion and the MOB-MOMDP criterion apply slightly different forms of discounting. However, for sufficiently large γ , the difference is small enough to ensure that the criteria are either equivalent or approximately equivalent, resulting in optimal or quasi-optimal HILMO policies.

Note that the optimal HILMO policy constructed above executes at the smallest possible temporal scale, *i.e.*, the high-level policy π^T selects goal poses which are directly adjacent to the agent's current pose, and the low-level policy π^{χ} is able to reach such goal poses in a single timestep. However, this does not preclude the existence of other optimal HILMO policies which execute at broader temporal scales, in which the high-level policy selects goal poses which require multiple timesteps to be reached.

This analysis is limited to *deterministic* MOB-MOMDPs and does not intrinsically carry over to *stochastic* MOB-MOMDPs. In Appendix E, we extend the analysis, providing a highly stochastic MOB-MOMDP example which demonstrates issues with the HILMO approach and a lowly stochastic MOB-MOMDP, which demonstrates that such issues are minor if the stochasticity is also minor. We argue that because most realistic MOB-MOMDPs have a relatively low amount of stochasticity, the HILMO approach should still be able to achieve theoretically quasi-optimal performance even in mildly stochastic MOB-MOMDPs.

5 Related Work

This section describes prior works on hierarchical reinforcement learning (HRL).

HRL for MDPs. For discrete action spaces, several prior works [6,14] addressed learning hierarchically. For continuous action spaces, HAC [16] and HIRO [20] proposed a hierarchical agent consisting of policies learned jointly in an off-policy manner. HIPPO [17] is an on-policy hierarchical agent but focuses more on optimizing pre-trained skills for downstream tasks.

HRL for POMDPs. Hierarchical Suffix Memory [11] incorporated hierarchies with memories to solve navigation tasks under perceptual aliasing. Another twolevel hierarchical agent [15] used hand-crafted goals with policies learned independently. HQ-Learning [28] solved specific POMDPs using a pre-specified number of sequentially chained reactive sub-agents. [25] combined hardcoded memoryless options (temporally extended actions) to solve a navigation POMDP by conditioning each option on the previous one. In contrast to these works, which use hardcoded bottom-level policies, hand-crafted goals, and have rigid structures, our hierarchical agent learns policies of all levels jointly, can handle continuous control tasks, and is supported by theoretical analysis.

6 Experiments

We perform experiments on continuous control tasks including two navigation and two manipulation domains implemented in MuJoCo [26]. Below in Table 1, we describe each domain and the corresponding state and observation.

6.1 Domains

Two-Boxes. A finger is velocity-controlled $(\dim(\mathcal{A}) = 1)$ on a 1D track to perform a dimension check of two boxes (Fig. 4a). Since the finger is always compliant, it will be deflected from the vertical axis when it glides over a box. The agent observes the finger's position and angle $(\dim(\Omega) = 2)$ but not the positions of the two boxes. Therefore, an optimal agent must localize *both* boxes and determine their sizes using the history of angles and positions. When the two boxes have the same size, the agent must go to the right end (pink) to get a non-zero reward and otherwise to the left end. The agent receives a penalty if



Fig. 4: Four continuous control domains in MuJoCo [26] to perform experiments.

Table 1: State, goal, and observation descriptions. x^g is the goal used by the bottom-level policy in the hierarchical agents (HILMO, HILMO-O, and HAC).

Domain	Description
Two-Boxes	$x, x^g {:}$ finger positions, $y {:}$ desired target position, $z {:}$ finger angle
Ant-Heaven-Hell	x: joint angles and velocities, and body position, x^{g} : ant body position, y: heaven position, z: heaven position or null
Ant-Tag	x: joint angles and velocities, and body position, x^g : ant body position, y: opponent position , z: opponent position or null
Door-Push	$x:$ joint angles and velocities, $x^g\colon$ target joint angles, $y:$ push direction, $z:$ door angle

reaching wrong ends. An episode terminates whenever the two ends are reached, or lasts more than 100 timesteps.

Ant-Heaven-Hell. An ant with four legs $(\dim(\mathcal{A}) = 8)$ moving in a 2D Tshaped world will receive a non-zero reward by reaching a green area (heaven) that can be on the left or the right corner (Fig. 4b) of a junction. The ant receives a penalty when entering a red area (hell). When it stays in the blue ball, it can observe heaven's side (left/right/null). Here the observation includes the joints' angles & velocities of the four legs and the side indicator (dim(Ω) = 30). The ant starts randomly around the bottom corner, and an episode terminates when heaven or hell is reached, or more than 400 timesteps have passed. An optimal agent must visit the blue region to observe heaven's side, memorize the side while going to heaven, and finally goes to heaven.

Ant-Tag. The same ant now has to search and "tag" a moving opponent by being sufficiently close to it (having the opponent inside the green area centered at the ant in Fig. 4c) to get a non-zero reward. Both start randomly but not too close to each other. The opponent follows a fixed stochastic policy, moving a constant distance away from the ant 75% of the time or staying otherwise. An observation includes the joints' angles & velocities of four legs and the 2D coordinate of the opponent (dim(Ω) = 31), containing the opponent's position only when it is inside the visibility (blue) area centered at the ant. An episode terminates when the opponent is tagged, or more than 400 timesteps have passed.

Door-Push. A 3-DoF gripper $(\dim(\mathcal{A}) = 3)$ in 3D must successfully push a door to receive a non-zero reward (Fig. 4d). The door, however, can only be pushed in one direction (front-to-back or vice versa), and the correct push direction is unknown to the agent. Here the agent can observe the joints' angles and velocities and the door's angle $(\dim(\Omega) = 7)$. Starting each episode, the door is present to the gripper, initialized with a random pose. An optimal agent must experiment to determine the correct push direction. For example, when it fails to open the door in one direction, it must go to the other side of the door while memorizing the previous push direction that did not work, not to try that again. Therefore, an optimal agent must infer the correct push direction from the history of observations. An episode terminates when the door's angle is larger than a threshold or more than 400 timesteps have passed.

6.2 Agents

We consider the following hierarchical (H) and flat (F) agents:

- (H) A two-level HILMO (ours) agent with goals x^g described in Table 1.
- (H) A two-level HAC [16] agent with the same goal as in HILMO to show that recurrence is needed for a hierarchical agent to solve our domains.
- (H) HILMO-O (ours) same structure and goals as HILMO, but implemented using the HIRO [20] framework with off-policy corrections (see Appendix F for the algorithm) to replace HATs. Another difference is that the bottom policy of HIRO originally receives dense instead of sparse rewards, *i.e.*, $R^{\mathcal{X}}(x', x^g) = -d(x', x^g)$, hence HGTs are not used. Plus, there is no penalty for unachieved goals by the top policy (STTs are not used either). Like HAC, HIRO is a common hierarchical baseline for continuous control.
- (F) Soft Actor-Critic (SAC) [8] with observations instead of states to show that even a strong flat agents cannot solve our domains without memory.
- (F) Recurrent Soft Actor-Critic (RSAC) [30] is a recurrent version of SAC.
- (F) Discriminative Particle Filter Reinforcement Learning (DPFRL) [19] is an on-policy agent that summarizes the history using a differentiable particle filter. DPFRL is one of state-of-the-art model-free POMDP methods.
- (F) Variational Recurrent Model (VRM) [9] is one of state-of-the-art offpolicy model-based agents. It solves POMDPs by using a recurrent variational dynamic model and an SAC agent.
- (F) Addition baselines are explored in Appendix G.

6.3 Learning Performance

We compare the success rates and the wall-clock training time of all agents. We alternate training and testing for all agents and compute the average success rates over 100 test episodes for every 2000 environment timesteps.

Success Rates. For HILMO agents, we only report the best performance achieved with a specific strategy to create top-level observations (Full, Final, or

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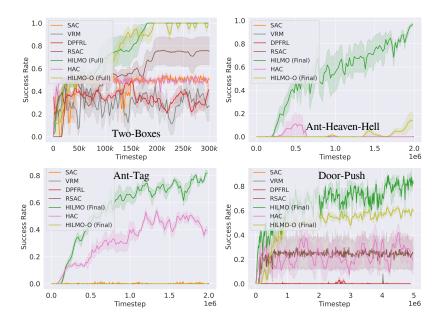


Fig. 5: Success rate means and standard deviations (4 seeds).

Recurrent). From Fig. 5, we can see that across all domains, HILMO consistently outperforms all flat baselines and is on par or better than HILMO-O. Moreover, HILMO is the only agent that can learn well in Ant-Heaven-Hell and Ant-Tag.

Efficient Exploration. We hypothesize that HILMO performs better because of a more effective exploration. To validate, we visualize the ant's positions in Ant-Heaven-Hell during 500k environment timesteps of training in Fig. 6. Apparently, HILMO explores better thanks to high-level actions, covering the T-shaped space densely.



Fig. 6: Coverage of HILMO, HILMO-O, and RSAC in Ant-Heaven-Hell after 500k timesteps of training.

HILMO-O also utilizes high-level actions, but its bottom policy rarely achieves given goals, which is detrimental to the final performance. The reason is that without penalizing unachieved goals, the top policy of HILMO-O is free to propose unrealistic goals (*e.g.*, outside of the working space). This issue is also present in the original HIRO agents (see this hyper-link). In Two-Boxes and Door-Push, the bottom policy of HILMO-O performs better, therefore, its performance is relatively comparable to that of HILMO.

<u>Other Baselines.</u> With no memory, SAC could not solve any domains as expected. Surprisingly, a memory-less HAC can perform quite well in Ant-Tag due to a well-trained bottom policy that sometimes can corner and tag the opponent. RSAC can only succeed in Two-Boxes for some seeds. It struggles to learn in the

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Domain	RSAC	HILMO-O	HILMO
Two-Boxes	3.31 ± 0.2	0.96 ± 0.2	1.04 ± 0.3
Ant-Heaven-Hell	71.02 ± 0.3	11.31 ± 0.2	$\textbf{4.69} \pm \textbf{0.3}$
Ant-Tag	68.25 ± 0.4	12.51 ± 0.3	$\textbf{6.41} \pm \textbf{0.3}$
Door-Push	112.7 ± 0.4	26.10 ± 0.2	$\textbf{23.2}\pm\textbf{0.2}$

Table 2: Wall-clock training time in *hours* for selected agents in Fig. 5.

other tasks in which episodes last longer, and the reward sparsity will hinder learning more severely. DPFRL and VRM surprisingly perform poorly across domains. These methods have no mechanisms to deal with sparse rewards and were tested only on POMDPs that require no active information gatherings (*e.g.*, flickering Atari games, or locomotion tasks with hidden velocities or positions).

Wall-clock Training Time. To measure the time fairly, we train only one experiment at a time on the same CPU (Intel i7-8700K 3.7GHz with 12 processors) and GPU (Nvidia GeForce GTX 1080 8GB). Moreover, we excluded other baselines that did not learn or use GPU in their implementations. Table 2 shows that our agents (HILMO and HILMO-O) take significantly less time to train than RSAC in all domains. While they are relatively comparable in Two-Boxes, HILMO-O is slower than HILMO in the remaining three domains. In these domains, while RSAC does not learn after days of training, HILMO can learn good policies in a reasonable time. The acceleration can be attributed to shorter top-level episodes for HILMO because each top-level observation summarizes several primitive observations. Moreover, the bottom policy trained in parallel can learn significantly faster due to full observability (see Appendix H).

6.4 Comparing Full, Final, and Recurrent

The comparison is depicted in Fig. 7. Generally, *Final* (red) is the best strategy, potentially due to more concise information. It dominates in three out of four domains, only be outperformed by *Full* (green) in Two-Boxes. *Final* does not perform well in Two-Boxes possibly because the proposed goals must be precisely on top of the two boxes for the final observation to contain angular changes. In contrast, other strategies are less restricted. *Recurrent* (purple) introduces another recurrent component into the agent, which seems to hinder learning.

6.5 Robot Experiments for Two-Boxes

The learned policy is deployed on a UR5e robot arm (Fig. 8 left) with a specialized gripper [24] that can control the compliance of its two fingers using hydrostatic actuators. However, we only use the left finger and keep it compliant at all times. We adjust the distance between the fingertip and the table so that deflected angles behave similarly in the simulation. We use wooden boxes of two sizes, making up four configurations, and perform three runs for each

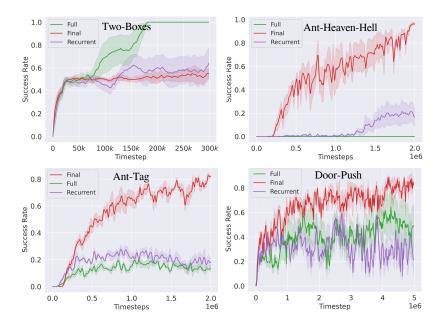


Fig. 7: Comparing the success rates of different top-level observations (4 seeds).

configuration with a random initial position of the finger between the two boxes. All runs are successful. Please refer to https://youtu.be/KiVIBkdm0U8 for the demonstration of the policy as well as the policies learned in other domains.

Policy Visualization. The right side of Fig. 8 illustrates the policy learned by our agent in Two-Boxes with two configurations of boxes: small-small and small-big. The learned policy generates both informative and rewarding actions based on the history of the left finger's angles and positions. The agent first goes right until passing a box; then, it backtracks until passing the other box. If the angle history indicates that the two boxes have the



Fig. 8: (Left) A UR5e robot and wooden boxes to deploy the learned policy. (Right) The policy learned in Two-Boxes with two distinct box configurations. White circles denote goals generated by the top-level policy.

same size, the agent will go to the right end through goal 6 in case A to finish the task. Otherwise, it will go to the left end through goal 4 in case B. In Ant-Heaven-Hell, we also notice interesting patterns when visualizing the evolution of cell memories of a trained HILMO agent (see Appendix I).

7 Conclusion and Future Work

This work introduces MOB-MOMDPs, a subclass of MOMDPs which can be found all across active robotic research areas, in which the agent's actions only have a direct effect on the fully observable component of the state. We also introduce HILMO, a hierarchical agent that exploits the mixed observability assumptions of MOB-MOMDPs. Our empirical evaluation shows that HILMO achieves improved learning performance and training time. A policy learned entirely in simulation is effectively deployed on real hardware.

Even we focus on continuous control tasks, extending our approach for discrete control tasks is straightforward. Moreover, a hierarchical agent further allows state abstractions in which the input might be optimized for each level for more efficient learning. For instance, the top policy can propose optimal goals in Ant-Tag and Ant-Heaven-H ell without using the joints' angles and velocities.

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